Machine Learning and Knowledge Graphs: possible issues to be taken into account

Claudia d'Amato

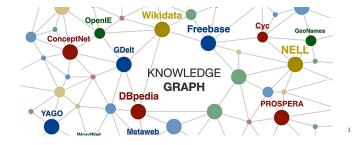
Department of Computer Science University of Bari

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Introduction



Open KG online with content freely accessible

- BabelNet
- DBpedia
- Freebase
- Wikidata
- YAGO
- ...

Enterprise KG for commercial usage

- Google
- Amazon
- Facebook
- LinkedIn
- Microsoft

picture from https://www.csee.umbc.edu/courses/graduate/691/fall19/07/1 > < 🗇 > < 🖹 > < 🖹 > 🛬 🔊 🤇 🔿

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Knowledge Graph: Definition [Hogan et al., 2021]

A graph of data intended to convey knowledge of the real world

- conforming to a graph-based data model
- nodes represent entities of interest
- edges represent potentially different relations between these entities
- data graph potentially enhanced with schema

KGs: Main Features

- grounded on the Open World Assumption (OWA)
- ontologies employed to define and reason about the semantics of nodes and edges
- very large data collections
- suffer of *incompleteness* and *noise*
 - since often result from a complex building process
- RDF, RDFS, OWL representation languages will be assumed

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Machine Learning & Knowledge Graphs



Two perspectives:

• KG as input to ML

• **Goal:** improving the performance in many learning tasks, e.g. QA, image classification, instance disambiguation, etc.

• ML as input to KG

- Goal: improving the KG itself
 - enriching the schema/ontology
 - creating new facts
 - creating generalizations
 - prototyping
 - $\bullet\,$ improving the size, coverage, depth and accuracy of KGs $\rightarrow\,$ reducing their production costs

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Machine Learning: the study of systems that improve their behavior over time with experience [Mitchell, 1997; MacKay, 2002; Flach, 2012; Murphy, 2012] experience:

- interactions with the world
- set of *observations* or *examples*
- internal states and processes

Approaches: [Luger, 2005]

- symbol-based
- connectionist / neurally inspired / numeric

Symbol-Based Learning

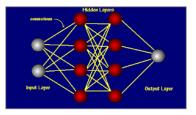
- uses symbols for representing entities and relationships of a problem domain (observations/examples)
- infer novel, valid and useful generalizations of examples
 - that provide new *insights* into the data/examples
 - are ideally readily *interpretable* by the user
- by *searching* thought possible generalizations expressed with symbols

Induction typically adopted

Neurally Inspired Learning

• represents knowledge as patterns of activity in networks of small, individual processing units

- needs to encode knowledge into numerical quantities in the network
- learns by *modifying* / adapting the network structure and weights in response to incoming (training) data
 - does not learn by adding representation to the KB



ML as input to KG

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Numeric-based methods

- highly scalable
- schema level information and reasoning capabilities almost disregarded

Knowledge Graph Refinement

- Link Prediction: predicts missing links between entities
- Triple Classification: assesses statement correctness in a KG

Symbol-based methods

- able to exploit background knowledge and (deductive) reasoning capabilities
- limited in scalability



Ontology Mining

• All activities that allow for discovering hidden knowledge from ontological KBs

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[d'Amato, 2020]

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Numeric-based methods

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Next Talk on Thursday

Symbol-based methods

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Ontology Mining

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Symbol-based Methods for Ontology Mining

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Ontologies act as a shared vocabulary for assigning data semantics

• Largely adopted in Semantic Web with the goal of making data on the Web machine understandable



Examples of existing real ontologies

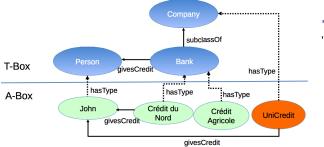
- Schema.org
- Gene Ontology
- Foundational Model of Anatomy ontology
- Financial Industry Business Ontology (by OMG Finance Domain Task Force)
- GoodRelations

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C. d'Amato (UniBa)

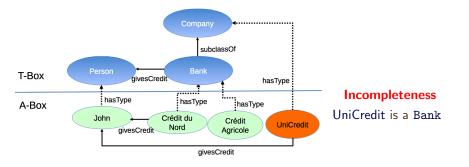
OWL standard language \Rightarrow Description Logics (DLs) theoretical foundation

Ontologies equipped with deductive reasoning capabilities \Rightarrow allowing to make explicit, knowledge that is implicit within them



Deduction: "Crédit du Nord", "Crédit Agricole" are also Company

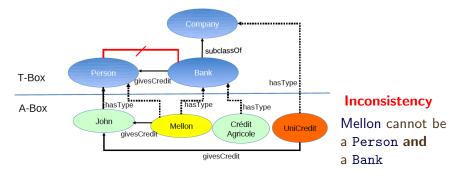
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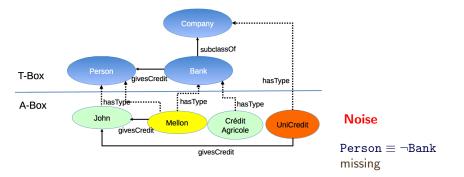
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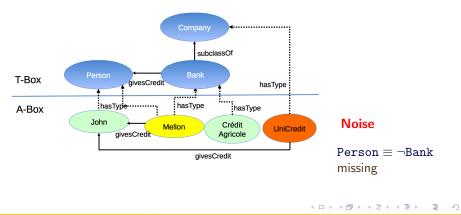
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ML methods adopted to discover new/additional knowledge by exploiting the evidence coming from the assertional data [d'Amato et al., 2010; d'Amato, 2020]

grounded on inductive approach



Motivation

Induction vs. Deduction

Deduction (Truth preserving)

Given:

- a set of general axioms
- a proof procedure

Draw:

• correct and certain conclusions

Induction (Falsity preserving)

Given:

a set of examples

Determine:

- a *possible/plausible* generalization covering
 - the given examples/observations
 - new and not previously observed examples

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Ontology Mining Tasks

- Instance Retrieval (Instance Level)
- Ontology Enrichment (Schema Level)

from an inductive perspective

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Ontology Mining Tasks

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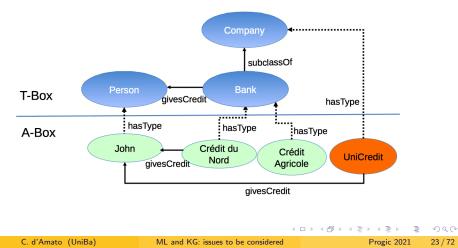
Instance Retrieval as a Classification Problem

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Introducing Instance Retrieval I

Instance Retrieval \rightarrow Finding the extension of a query concept

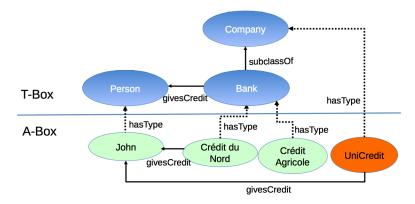
• Instance Retrieval (Bank) = {"Crédit du Nord", "Crédit Agricole" }



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Introducing Instance Retrieval I

Problem: Instance Retrieval in incomplete/inconsistent/noisy ontologies

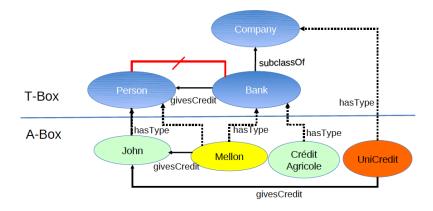


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Introducing Instance Retrieval II

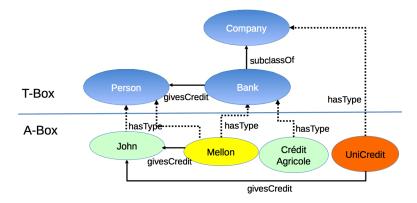
Problem: Instance Retrieval in incomplete/<u>inconsistent</u>/noisy ontologies



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Introducing Instance Retrieval III

Problem: Instance Retrieval in incomplete/inconsistent/noisy ontologies



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Idea

Casting the problem as a classification problem

assess the class membership of individuals in a DL KB w.r.t. the query concept

Similarity-based methods mostly adopted \Rightarrow efficient and noise tolerant

Issues: State of art classification methods cannot be straightforwardly applied

- generally applied to *feature vector* representation
 → upgrade DL expressive representations
- implicit Closed World Assumption made in ML
 → cope with the Open World Assumption made in DLs
- classes considered as *disjoint*
 - ightarrow cannot assume disjointness of all concepts

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Adopted Solutions:

- Defined new semantic similarity measures for DL representations [d'Amato, 2007]
 - to cope with the high expressive power of DLs
 - to deal with the semantics of the compared objects (concepts, individuals, ontologies)
 - to convey the underlying semantics of KB
- Formalized a set of criteria that a similarity function has to satisfy for being defined *semantic* [d'Amato *et al.*, 2008a]
- Definition of the classification problem taking into account OWA
- Multi-class classification problem decomposed into a set a smaller classification problems

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Definition (Problem Definition)

Given:

- ullet a populated ontological knowledge base $\mathit{KB} = (\mathcal{T}, \mathcal{A})$
- a query concept Q
- a training set with $\{+1, -1, 0\}$ as target values

Learn a classification function f such that: $\forall a \in Ind(A)$:

- f(a) = +1 if a is instance of Q
- f(a) = -1 if a is instance of $\neg Q$
- f(a) = 0 otherwise (unknown classification because of OWA)

Dual Problem

- given an individual $a \in Ind(A)$, tell concepts C_1, \ldots, C_k in KB it belongs to
- the multi-class classification problem is *decomposed* into a set of *ternary classification problems* (one per target concept)

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Developed methods

Pioneering the Problem

• relational K-NN for DL KBs [d'Amato et al., 2008b]

Improving the efficiency

• kernel functions for kernel methods to be applied to DLs KBs [Fanizzi and d'Amato, 2006; Fanizzi *et al.*, 2012a; Bloehdorn and Sure, 2007]

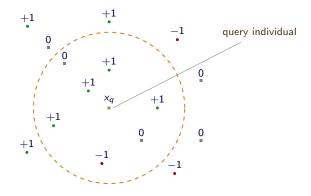
Scaling on large datasets

• Statistical Relational Learning methods for large scale and data sparseness [Huang *et al.*, 2010; Minervini *et al.*, 2015]

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Example: Nearest Neighbor Classification

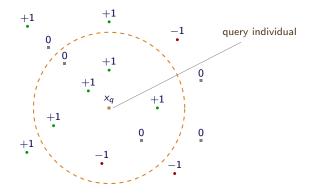
query concept: Bank k = 7 target values standing for the class values: $\{+1, 0, -1\}$



 $class(x_q) \leftarrow ?$

Example: Nearest Neighbor Classification

query concept: Bank k = 7 target values standing for the class values: $\{+1, 0, -1\}$



 $class(x_q) \leftarrow +1$

On evaluating the Classifier

Problem: How evaluating classification results?

- Inductive Classification compared with a standard reasoner (Pellet)
- Query concepts from ontologies publicly available considered
- Registered *mismatches*: <u>Induction</u>: $\{+1, -1\}$ <u>Deduction</u>: no results
- Evaluated as mistake if precision and recall were used while it could turn out to be a correct inference when judged by a human

Defined new metrics to distinguish induced assertions from mistakes

		Reasoner		
		+1	0	-1
INDUCTIVE	+1	М	1	С
CLASSIFIER	0	0	М	0
	-1	С	1	М

M Match Rate C Commission Error Rate

Ommission Error Rate

/ Induction Rate

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ML and KG: issues to be considered

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Lesson Learnt from experiments

- Commission error almost zero on average
- Omission error rate very low and only in some cases
 - Not null for ontologies in which disjoint axioms are missing
- Induction Rate not zero
 - new knowledge (not logically derivable) induced ⇒ can be used for semi-automatizing the ontology population task
 - induced knowledge ⇒ individuals are instances of many concepts and homogeneously spread w.r.t. the several concepts.

	match	commission	omission	induction
SWM	97.5 ± 3.2	0.0 ± 0.0	2.2 ± 3.1	0.3 ± 1.2
LUBM	99.5 ± 0.7	0.0 ± 0.0	0.5 ± 0.7	0.0 ± 0.0
NTN	97.5 ± 1.9	0.6 ± 0.7	1.3 ± 1.4	0.6 ± 1.7
FINANCIAL	99.7 ± 0.2	0.0 ± 0.0	0.0 ± 0.0	0.2 ± 0.2

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Research Directions to Investigate Further

• Multi-Label Classification

- individuals can be instance of more than one concept at the same time [Melo and Paulheim, 2019; Peixoto *et al.*, 2016]
- Hierarchical Classification
 - Particularly appropriate for type prediction [Melo et al., 2016, 2017]
- Ensemble methods
 - only boosting has been preliminarily applied [Rizzo *et al.*, 2015a; Fanizzi *et al.*, 2019]
- Regression
 - to be exploited for predicting missing values of datatypes properties [Fanizzi *et al.*, 2012b; Rizzo *et al.*, 2016]

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Ontology Mining Tasks

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- Ontology Enrichment (Schema Level)

from an inductive perspective

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Ontology enrichment as a Concept Learning Problem

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On Learning Concept Descriptions I

Goal: Learning descriptions for a given concept name / expression

 $Example: Man \equiv Human \sqcap Male$

Question: How to learn concept descriptions automatically, given a set of individuals?

Idea

Regarding the problem as a *supervised concept learning* task

Supervised Concept Learning:

- Given a training set of positive and negative examples for a concept,
- *construct* a *description* that will accurately classify whether future examples are positive or negative.

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On Learning Concept Descriptions II

Definition (Problem Definition)

• Given

- $\bullet\,$ the KB ${\cal K}$ as a background knowledge
- a subset *pos* of individuals as positive examples of *C*
- a subset *neg* of individuals as negative examples of C

Learn

- a DL concept description D so that
- the individuals in *pos* are instances of *D* while those in *neg* are not

The Learning Process: Learning as Search

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How Does Relational Learning Work?

Symbolic ML techniques essentially search a space of possible hypothesis \mathcal{L}_h (e.g. patterns, models, regularities) [De Raedt, 2008]

- Depending on the task, <u>different search algorithms</u> and principles <u>apply</u>
 - *complete search* strategy applicable
 - *heuristic search* method (e.g. *hill climbing*)
- easy way: generate-and-test algorithm
 - naïve and inefficient

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A Generate-and-Test Algorithm

A (trivial) algorithm based on a *generate-and-test* technique is the **enumeration algorithm**

• for each possible hypothesis h checks if h satisfies a given quality criterion Q wrt the data D

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for each h \in \mathcal{L}_h do
if Q(h,D) = true then
output h
end if
end for
```

Properties

- whenever a solution exists, the enumeration algorithm will find it
- it can only be applied if the hypotheses language \mathcal{L}_h is *enumerable*
- the algorithm searches the whole space \rightarrow inefficient
 - it is advantageous to *structure* the search space, according to *generality* allowing for its *pruning*

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Usually logical entailment used as for generality relation

- a more general hypothesis logically entails the more specific one
- a more specific hypothesis is a *logical consequence* of the more general one

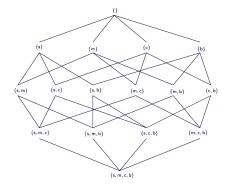
Definition (generality)

Let $h_1, h_2 \in \mathcal{L}_h$. Hypothesis h_1 is more general than (or equivalent) hypothesis h_2 , $h_1 \leq h_2$, iff all examples covered by h_2 are also covered by h_1 , i.e., $c(h_2) \subseteq c(h_1)$

- We also say that
 - h_2 is a *specialization* of h_1
 - h_1 is a *generalization* of h_2

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• h_1 is a proper generalization of h_2, h_1 \prec h_2
when h_1 \preceq h_2
and h_1 covers examples not covered by h_2
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Space traversed in:

- a *general-to-specific* strategy:
 - the algorithm starts from the *most general hypothesis*
 - then repeatedly specializes mapping hypothesis /patterns onto a set of specializations

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• a *specific-to-general* strategy

Notice that the \leq is transitive and reflexive; \rightarrow it is a *quasi-order*

- not anti-symmetric since *there may exist several hypotheses that cover* exactly the same set of examples: *syntactic variants*
 - undesirable: they introduce redundancies in the search space

Monotonicity I

The generality relation imposes a useful structure on the search space provided that the quality criterion involves some properties:

Definition (monotonicity of the criteria)

A quality criterion Q is **monotonic** iff

$$\forall s,g \in \mathcal{L}_h, \forall D \subseteq \mathcal{L}_e \colon (g \preceq s) \land \ Q(g,D) \rightarrow Q(s,D)$$

It is anti-monotonic iff

$$\forall s,g \in \mathcal{L}_h, \forall D \subseteq \mathcal{L}_e \colon (g \preceq s) \land \ Q(s,D) \rightarrow Q(g,D)$$

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Monotonicity II

Properties that directly follow from the definitions of monotonicity and anti-monotonicity:

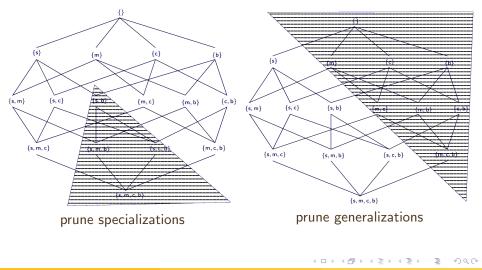
Property (prune generalizations)

If a hypothesis h does not satisfy a monotonic quality criterion then none of its generalizations will

Property (prune specializations)

If a hypothesis **h** does not satisfy an anti-monotonic quality criterion then none of its specializations will

Monotonicity III



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ML and KG: issues to be considered

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Refinement Operators I

How can be the search space \mathcal{L}_h traversed?

Many ML algorithms are based on refinement operators

 generating sets of specializations (or generalizations) of given hypotheses

Definition

A generalization operator $\rho_g \colon \mathcal{L}_h \to 2^{\mathcal{L}_h}$ is a function such that

$$\forall h \in \mathcal{L}_h \colon \rho_g(h) \subseteq \{h' \in \mathcal{L}_h \mid h' \preceq h\}$$

Dually, a specialization operator $\rho_s: \mathcal{L}_h \to 2^{\mathcal{L}_h}$ is a function such that

$$\forall h \in \mathcal{L}_h \colon \rho_s(h) \subseteq \{ h' \in \mathcal{L}_h \mid h \preceq h' \}$$

Refinement Operators II

Properties

defined for specialization op's (corresponding definitions for generalization op's easily obtained)

- ρ is an **ideal operator** for \mathcal{L}_h iff $\forall h \in \mathcal{L}_h : \rho(h) = \min(\{h' \in \mathcal{L}_h \mid h \prec h'\})$
 - it returns all children for a node in the Hasse diagram
 - proper refinements, not a syntactic variant of the original hypothesis
 - often are used in *heuristic search* algorithms
- ρ is an **optimal operator** for L_h iff for all $h \in \mathcal{L}_h$ there exists exactly one sequence of hypotheses $T = h_0, h_1, \ldots, h_n = h \in \mathcal{L}_h$ such that $h_i \in \rho(h_{i-1})$ for all i
 - used in *complete search* algorithms
- An operator for which there exists at least one sequence from ⊤ to any h ∈ L_h is called complete
- An operator for which there exists *at most* one such sequence is **non-redundant**

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A Generic Learning Algorithm I

Adapting the enumeration algorithm to employ the refinement operators:

```
\begin{array}{l} \textit{Queue} \leftarrow \textit{Init} \\ \textit{Th} \leftarrow \emptyset \\ \texttt{while not Stop do} \\ \textit{Delete h from Queue} \\ \texttt{if } Q(h, D) \texttt{then} \\ \textit{Th} \leftarrow \textit{Th} \cup \{h\} \\ \textit{Queue} \leftarrow \textit{Queue} \cup \rho(h) \\ \texttt{end if} \\ \textit{Queue} \leftarrow \textit{Prune}(\textit{Queue}) \\ \texttt{end while} \\ \texttt{return Th} \end{array}
```

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A Generic Learning Algorithm II

Observations. many parameters determining the behavior

- Init determines the starting point of the search algorithm
 - The initialization may yield one or more initial hypotheses
 - Most algorithms start either at ⊤ and only specialize (the so-called general-to-specific systems), or at ⊥ and only generalize (the specific-to-general systems)
- Delete determines the search strategy
 - *first-in-first-out*: breadth-first search
 - last-in-first-out: depth-first search
 - *best hypothesis* (according to some criterion or heuristic): best-first algorithm
- ρ determines the size and nature of the *refinement steps* through the search space
- Stop determines when the algorithm halts

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A Generic Learning Algorithm III

- Some algorithms compute all elements, k elements or an approximation of an element satisfying Q
 - if all elements are desired, Stop equals $Queue = \emptyset$
 - when k elements are sought, it is |Th| = k
- Some algorithms *Prune* candidate hypotheses from *Queue*
 - *heuristic pruning* prunes away parts of the search space that appear to be uninteresting
 - *sound pruning* prunes away parts of the search space that cannot contain solutions
- As with other search algorithms in AI:
 - complete algorithms compute all elements of $Th(Q, D, \mathcal{L}_h)$
 - *heuristic* algorithms aim at computing one or a few hypotheses that score best w.r.t. a given heuristic
 - not guaranteeing that the best hypotheses are found

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Concept Learning in Description Logics

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DL Concept Learning – Problem Definition I

- given a KB $\mathcal{K} = \langle \mathcal{T}, \mathcal{A} \rangle$
 - a target concept C
 - a set of training instances partitioned as examples and counterexamples $E = E_+ \cup E_-$ for C

find a description *D* for *C* generalizing E, $C \equiv D$, that <u>maximizes</u> the *accuracy* w.r.t. the positive and negative examples

Possible Issues:

- Negative examples: ML grounded on CWA, DLs based on OWA
 - Learning from positive examples only if negative examples missing
- Suitable refinement operators needed
- Evaluating results: metrics, unbalanced setting

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DL Concept Learning – Problem Definition II

Accuracy

D correctly *entails* at least $(1 - \epsilon)|\mathsf{E}|$ of the assertions on examples regarding their membership to *C*: $\forall e \in \mathsf{E}_+ : \mathcal{K} \sqcup \{D\} \models C(e)$ and $\forall e \in \mathsf{E}_- : \mathcal{K} \sqcup \{D\} \not\models C(e)$

> stronger alternative: $\forall e \in \mathsf{E}_{-} : \ \mathcal{K} \sqcup \{D\} \models \neg C(e)$

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<u>Variant</u>: separate ϵ_+ and ϵ_-

Refinement Operators

Randomized recursive **refinement operator** ρ $C' \in \rho(C)$

- $C' = C \sqcap A$
- $C' = C \sqcap \neg A$
- $C' = C \sqcap \forall R.\top$
- $C' = C \sqcap \exists R. \top$
- $C' = C_1 \sqcap \cdots \sqcap B \sqcap \cdots \sqcap C_n$ if $C = C_1 \sqcap \cdots \sqcap A \sqcap \cdots \sqcap C_n$ and $B \sqsubseteq A$
- $C' = C_1 \sqcap \cdots \sqcap \neg B \sqcap \cdots \sqcap C_n$ if $C = C_1 \sqcap \cdots \sqcap \neg A \sqcap \cdots \sqcap C_n$ and $A \sqsupseteq B$
- $C' = C_1 \sqcap \cdots \sqcap \exists R.D \sqcap \cdots \sqcap C_n$ if $C = C_1 \sqcap \cdots \sqcap \exists R.E \sqcap \cdots \sqcap C_n$ and $D \in \rho(E)$
- $C' = C_1 \sqcap \cdots \sqcap \forall R.D \sqcap \cdots \sqcap C_n$ if $C = C_1 \sqcap \cdots \sqcap \forall R.E \sqcap \cdots \sqcap C_n$ and $D \in \rho(E)$

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Developed Methods for Supervised Concept Learning

• Separate-and-conquer approach

- YinYang [lannone et al., 2007]
- DL-FOIL [Fanizzi et al., 2008, 2018]
- DL-Learner [Lehmann and Hitzler, 2010]
- CELOE [Lehmann et al., 2011]
- DL-FOCL [Rizzo et al., 2020]

• Divide-and-conquer approach

- TermiTIS [Fanizzi et al., 2010]
- PARCEL [Tran et al., 2012]
- SPACEL [Tran et al., 2017]
- TermiTIS Extensions
 - Pruning Methods [Rizzo *et al.*, 2017b,a] simplify complexity & avoid overfitting
 - *Terminological Random Forests* TRFs [Rizzo *et al.*, 2015a] tackling also the *class-imbalance* problem
 - Evidential TDTs and TRFs [Rizzo et al., 2018, 2015b] based on the Dempster-Shafer Theory(DST): a general framework for reasoning with uncertainty

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DL-FOIL

Problem: simple generate-and-test algorithms may be inefficient

DL-FOIL adopt a heuristic *sequential covering* algorithm [Fanizzi *et al.*, 2008; Fanizzi, 2011]

general-to-specific search

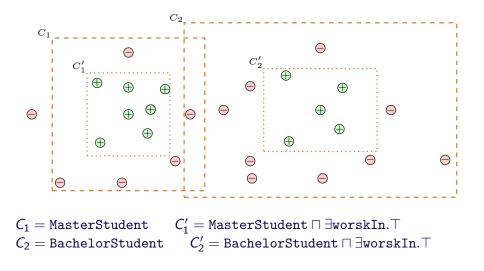
- starting from \top
- repeat (cover as many positives as possible)
 - if non positives are covered
 - repeat
 - find heuristically the best refinement
 - (not to cover them yet still covering as many positives as possible)
 - add refinement as a disjunct partial def.

until only positives covered

until all positives covered

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DL-FOIL II



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DL-FOIL III

Heuristic function: Gain

$$g(D_0, D_1) = p_1 \cdot \left[\log \frac{p_1}{p_1 + n_1 + u_1} - \log \frac{p_0}{p_0 + n_0 + u_0} \right]$$

where

- $p_1|n_1|u_1$ number of exs covered by the specialized def. D_1
- $p_0|n_0|u_0$ number of exs covered by the former (partial) def. D_0
- + correction via *Laplace smoothing*

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On Evaluating the Learnt Concept Descriptions

- Publicly available ontologies considered
- A number (30) of satisfiable randomly generated concepts considered
- Positive and negative examples collected for each concept by using a deductive reasoner
- Running concept learning on the collected positive and negative examples
- Inductive classification performed on the learnt concept descriptions

	match	commission	omission	induction
ontology	rate	error rate	error rate	rate
BioPax	76.9 ± 15.7	19.7 ± 15.9	7.0 ± 20.0	7.5 ± 23.7
NTN	78.0 ± 19.2	16.1 ± 4.0	6.4 ± 8.1	14.0 ± 10.1
Financial	75.5 ± 20.8	16.1 ± 12.8	4.5 ± 5.1	3.7 ± 7.9

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Examples of Learned Descriptions with DL-FOIL

```
induced:
Or( And( physicalEntity protein) dataSource)
original:
Or( And( And( dataSource externalReferenceUtilityClass)
ForAll(ORGANISM ForAll(CONTROLLED phys icalInteraction)))
protein)
NTN
induced:
Or( EvilSupernaturalBeing Not(God))
original:
Not(God)
FINANCIAL
induced:
Or( Not(Finished) NotPaidFinishedLoan Weekly)
original:
Or( LoanPayment Not(NoProblemsFinishedLoan))
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                         ML and KG: issues to be considered
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```

Lesson Learnt from Experiments

- Relatively small ontological KBs adopted ⇒ scalability needs to be improved
- Suitable concept descriptions learned ⇒ validation by expert recommended for adding axioms to the KB
 - approximated descriptions may be learned depending of the threshold

Conclusions

Machine Learning methods

- could be usefully exploited for ontology mining
- suitable also in case of incoherent/noisy KBs
- can be seen as an additional layer on top of deductive reasoning for *new/additional forms of approximated reasoning capabilities*

Adopting ML solutions could be simple in principle

- often instantiating an existing learning schema is just needed
- Alert
 - understand the meaning of each component for instantiating a learning schema correctly
 - it could be the case that some components require newly developed solutions
 - e.g. new similarity measure for expressive representations, suitable refinement operators

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That's all!

Questions ?

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